

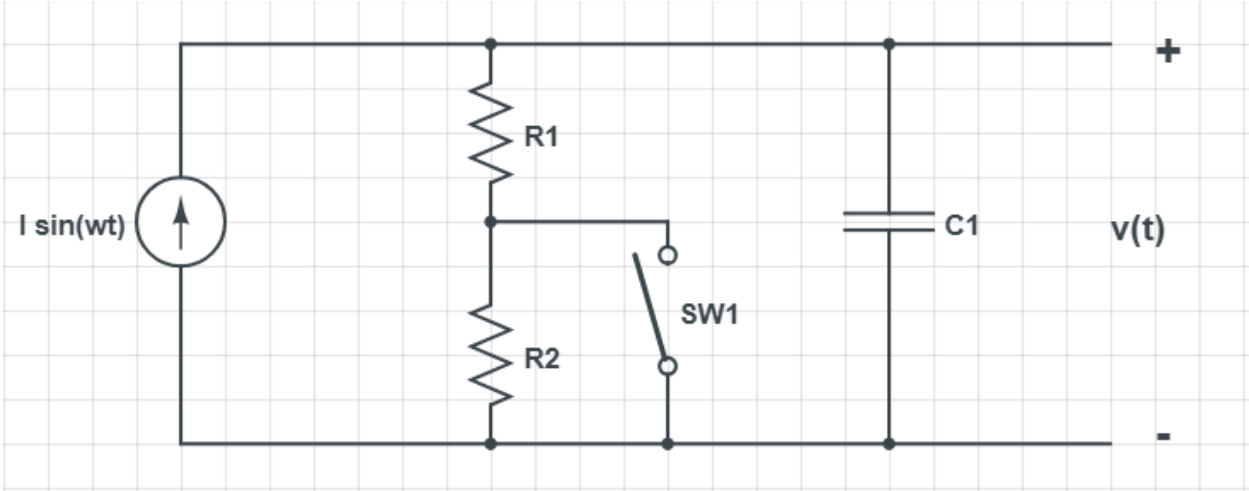
**Fall 2018: EE-240 Circuits I**  
**Assignment # 05**  
**Due Date: 06 December 2018, Thursday**

**Please read the following instructions:**

- Submit the assignment on A-4 sheets bound together. Please note that assignments submitted from torn notebook pages will not be accepted.
- You are required to submit the assignment at the start of class on the due date. Late submissions will not be accepted.
- Please ensure that you have clearly written your name and roll numbers on the assignment.
- The assignment is long, so you are advised to start as soon as possible. Please note that no deadline extension requests will be entertained.
- You are aware of the LUMS honor code and therefore, any plagiarism attempts will be directly reported to the **Disciplinary Committee**. If you are facing any difficulties or have questions, ask the course staff (Instructor/TA), they are there to help you.

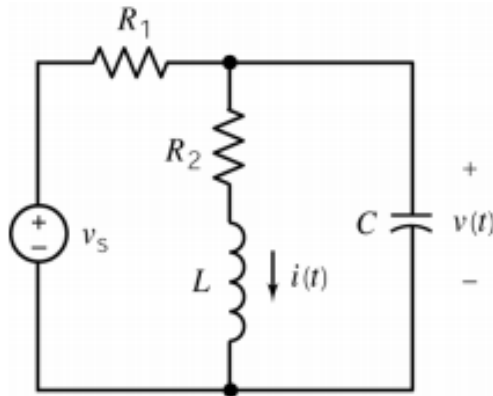
The total marks for the assignment are **100**.

Q1: The switch SW1 is opened for a long time until the network is in steady state. At  $t=0$ , the switch is closed. Find  $v(t)$  for  $t>0$ . [15]



Q2: Find a second-order differential equation in terms of  $R_1, R_2, L$  and  $C$  that represents this circuit. Suggest values of each component for which the system is: [10]

- a) Under-damped
- b) Over-damped

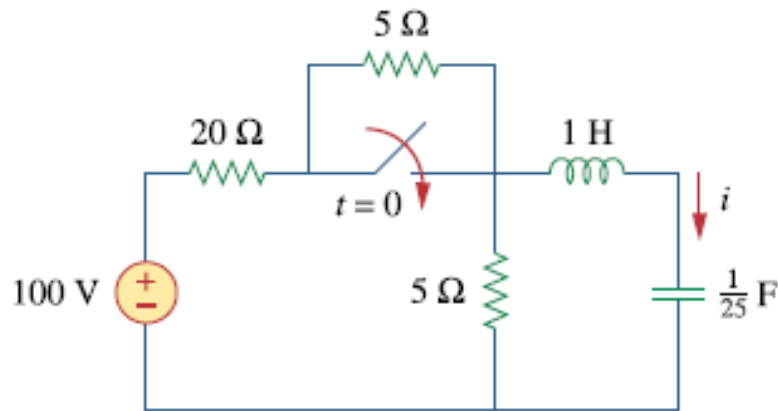


Q3: The current in a circuit is defined as  $d^2i(t)/dt^2 + 4di(t)/dt + 10i(t) = 0$ .

- a) Find the characteristic equation [2]
- b) What type of damping occurs in the circuit (with reasoning)? Draw its rough sketch. [3]
- c) Calculate  $i(t)$ ;  $i(0)=1$  and  $di(0)/dt=2$ . [5]

Q4: The circuit is in a steady state before the switch is closed at  $t=0$ . Find  $i(t)$  for  $t>0$ .

[15]



Q5: Solve the differential equations given below:

[5+5]

a)  $2(d^3i/dt^3) + 9(d^2i/dt^2) + 13(di/dt) + 6i = 0$

Where  $i(0^+)=0$ ,  $di/dt=1$  at  $t=0^+$

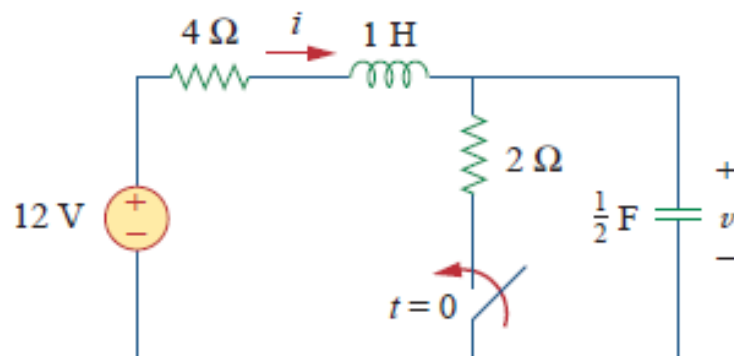
And  $d^2i/dt^2 = -1$  at  $t = 0^+$ .

b)  $d^2i/dt^2 + 3(di/dt) + 2i = 10\sin(10t)$

where  $i(0^+)=1$  and  $di/dt(0^+) = -1$ .

Q6: Find the complete response  $v(t)$  and then  $i(t)$  for  $t > 0$  in the circuit given below

[10]



Q7: The two equations that describe the given network are:

[15]

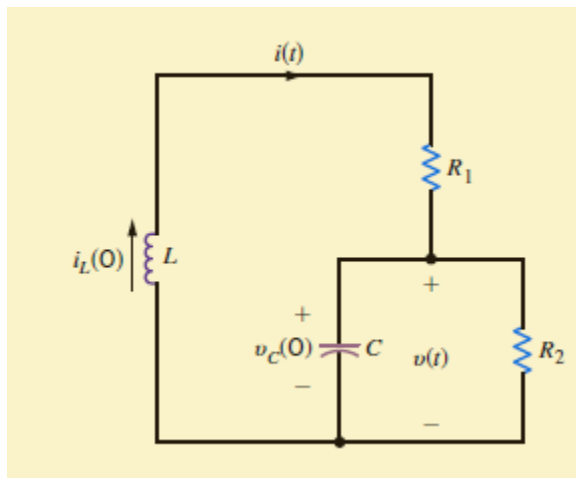
a)  $L \frac{di(t)}{dt} + R_1 i(t) + v(t) = 0$

b)  $C \frac{dv(t)}{dt} + v(t)/R_2 = i(t)$

Find expressions for  $i(t)$  and  $v(t)$

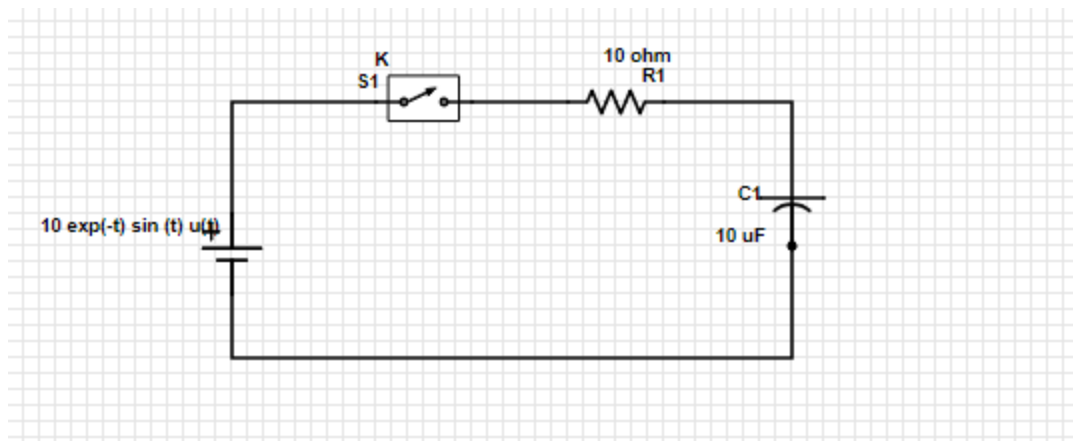
$R_1 = 10 \text{ ohm}$ ,  $R_2 = 8 \text{ ohm}$ ,  $C = 1/8 \text{ F}$ ,  $L = 2 \text{ H}$ ,  $v_C(0) = 1 \text{ V}$ ,  $i_L(0) = 0.5 \text{ A}$

NOTE: THIS IS A **VERY** TRICKY QUESTION



Q8: In the network given below, the switch K is closed at  $t=0$  with the capacitor initially uncharged. Find  $i(t)$  for  $t > 0$ .

[10]



Q9: For the circuit given below, find it's:

[5]

- a) Resonant Frequency
- b) Bandwidth
- c) Quality Factor

Where  $R=2$  ohm,  $L= 1$  mH,  $C=0.4$  uF.

Note: Give units and don't write the answers directly!

